# **BPS Algebra 1 Planning Guide**

#### 1st Semester - Unit 1: Relationships with Quantities and Reasoning with Equations **Objectives Essential Ouestions** The student will be able to: • How can inverse operations be used to solve • Work with linear & exponential expressions multi-step equations and inequalities? O Need to be able to identify, interpret, & • How is solving an inequality similar and/or different explain parts of expressions & write in an than solving an equation? • How can multiple representations of the same equivalent form. O Use units as a way to understand problems problem be useful? and guide solutions of multi-step problems • How can the Law of Exponents help you rewrite an (ex: Dimensional Analysis) exponential expression so that it has a single base Create/Solve Equations with a positive exponent? O 1-variable • How do you interpret solutions to equations and inequalities as viable or not? O 2-variable (graph these) O Literal equations with basic 4 operations O Need to be able to identify, interpret, & **Mathematical Practices** explain parts of equations 1: Make sense of problems and persevere in solving them. 2: Reason abstractly and quantitatively. Show multiple representations using PETS 4: Model with mathematics. (Pictures, Equations, Tables, Story Problems) • Work with rational exponents & exponential 5: Use appropriate tools strategically. functions including positive, negative, and fractional 6: Attend to precision. 7: Look for and make use of structure. exponents (ex: ½, ¼, etc.) 8: Look for and express regularity in repeated reasoning.

# **Montana Core Standards**

# **Unit 1A Module 1: Relationships Between Quantities**

# N.Q.1, N.Q.2, N.Q.3

**N.Q.1:** Use units as a way to understand problems from a variety of contexts (e.g., science, history & culture), including those of Montana American Indians, and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.

N.Q.2: Define appropriate quantities for the purpose of descriptive modeling.

**N.Q.3:** Choose a level of accuracy appropriate to limitations on measurement when reporting quantities.

# Unit 1A Module 2: Exponents & Real Numbers

# N.RN.1, N.RN.2, N.RN.3

**N.RN.1:** Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation from radicals in terms of rational exponents.

**N.RN.2:** Rewrite expressions involving radicals and rational exponents using the properties of exponents.

**\*\*N.RN.3:** Explain why the sum or product of two rational numbers is rational; that the sum of a rational number and an irrational is irrational; and that the product of a nonzero rational number and an irrational number is irrational.

Strikethrough means that the standard appears in a later course. \*\*This is the 1st time students are seeing this ever. Develop this standard to an appropriate level for the class. The highlighted standards are ones that are included in the Montana Core Standards but not in the Go Math! curriculum and need to be supplemented.

# **Unit 1A Module 3: Expressions**

## A.SSE.1, A.SSE.2, N.Q.1, N.Q.2

A.SSE.1: Interpret expressions that represent a quantity in terms of its context.
 A.SSE.1a: Interpret parts of an expression, such as terms, factors, and coefficients.
 A.SSE.1b: Interpret complicated expressions by viewing one or more of their parts as a single entity.

**\*\*A.SSE.2:** Use the structure of an expression to identify ways to rewrite it.

**N.Q.1:** Use units as a way to understand problems from a variety of contexts (e.g., science, history & culture), including those of Montana American Indians, and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.

N.Q.2: Define appropriate quantities for the purpose of descriptive modeling.

#### Unit 1B Module 4: Equations & Inequalities in One Variable

#### N.Q.2, A.CED.1, A.CED.3, A.CED.4, A.REI.1, A.REI.3

N.Q.2: Define appropriate quantities for the purpose of descriptive modeling.

**A.CED.1:** Create equations and inequalities in one variable and use them to solve problems from a variety of contexts (e.g., science, history, & culture), including those of Montana American Indians. Include equations arising from linear and <del>quadratic</del> <del>functions, simple rational and</del> exponential functions.

**A.CED.3:** Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.

**A.CED.4:** Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations.

**A.REI.1:** Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

A.REI.3: Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.

# Unit 1B Module 5: Equations in Two Variables and Functions

# A.CED.2, A.REI.10, A.REI.11, F.IF.1, F.IF.2, F.IF.3, F.IF.5, F.BF.1, F.BF.2

**A.CED.2:** Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

**A.REI.10:** Understand the graph of an equation in two variables is the set of all solutions plotted in the coordinate plane, often forming a curve (which could be a line).

**\*\*A.REI.11:** Explain why the x-coordinates of the points where the graphs of the equations y = f(x) and y = g(x) intersect are the solution of the equations f(x) = g(x); find the solutions approximately, e.g., using technology to graph functions, make tables of values, or find successive approximations. Include cases where f(x) and/or g(x) are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.

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**\*\*F.IF.1:** Understand that a function from one set (called the domain) to the other set (called the range) assigns to each element of the domain exactly one element of the range. If *f* is a function and *x* is an element of its domain, then f(x) denotes the output of *f* corresponding to the input *x*. The graph of *f* is the graph of the equations y = f(x).

**\*\*F.IF.2:** Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notations in terms of a context.

**\*\*F.IF.3:** Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of integers.

**\*\*F.IF.5:** Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes.

F.BF.1: Write a function that describes a relationship between two quantities.

**\*\*F.BF.2:** Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations from a variety of contexts (e.g., science, history, and culture), including those from the Montana American Indian, and translate between the two forms.

1st Semester - Unit 2: Linear and Exponential Relationships		
<ul> <li>Objectives</li> <li>The student will be able to: <ul> <li>Write and graph linear equations in Standard, Slope-Intercept, and Point-Slope Forms</li> <li>Solve systems of equations and inequalities <ul> <li>Algebraically (substitution &amp; elimination methods)</li> <li>Graphically (make sure to show inequality constraints)</li> </ul> </li> <li>Identify key features of a function <ul> <li>Is it a function?</li> <li>Domain, range, notation, evaluate</li> <li>End behavior, intercepts, increase/decrease intervals</li> </ul> </li> <li>Determine if a function represents exponential growth or decay</li> <li>Use and write sequences <ul> <li>Recursive vs. Explicit</li> <li>Arithmetic is the same as linear, Geometric is the same as exponential</li> </ul> </li> </ul></li></ul>	<ul> <li>Essential Questions</li> <li>Which features are highlighted in each of the forms of a linear equation?</li> <li>How does the solution set of a system of equations differ from the solution set of a system of inequalities?</li> <li>Using function notation, how do you determine the dependent and independent variables?</li> <li>What key features help you determine if a function is exponential growth or decay?</li> <li>What is the relationship between Arithmetic and Geometric sequences and Linear and Exponential functions?</li> <li>What is the difference between Explicit and Recursive Formulas?</li> <li>Given a transformed equation, describe similarities and differences between the parent and the transformed function.</li> <li>What is the slope of a given line and how do you find it both graphically and algebraically?</li> </ul> Mathematical Practices <ul> <li>1: Make sense of problems and persevere in solving them.</li> <li>2: Reason abstractly and quantitatively.</li> <li>3: Construct viable arguments and critique the reasoning of others.</li> <li>4: Model with mathematics.</li> <li>5: Use appropriate tools strategically.</li> <li>6: Attend to precision.</li> <li>7: Look for and make use of structure.</li> <li>8: Look for and express regularity in repeated reasoning.</li> </ul>	

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#### **Unit 2A Module 6: Linear Functions**

#### A.CED.2, A.REI.1, F.IF.4, F.IF.6, F.IF.7, F.IF.9, F.BF.3, F.LE.2, F.LE.5

**A.CED.2:** Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

**A.REI.1:** Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

**\*\*F.IF.4:** For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums or minimums; symmetries; end behavior, and periodicity.

**F.IF.6:** Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.

**\*\*F.IF.7:** Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated ones.

\*\***F.IF.7a:** Graph linear <del>and quadratic</del> functions and show intercepts, <del>maxima, and minima</del>.

**\*\*F.IF.9:** Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).

**\*\*F.BF.3:** Identify the effect on the graph of replacing f(x) by f(x) + k, kf(x), f(kx) and f(x+k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expression for them.

**\*\*F.LE.2:** Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).

**\*\*F.LE.5:** Interpret parameters in a linear or exponential function in terms of a context.

## **Unit 2A Module 7: Building Linear Functions**

#### A.CED.2, A.REI.12, F.BF.1, F.BF.2, F.BF.4

**A.CED.2:** Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

**\*\*A.REI.12:** Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersections of the corresponding half-planes.

F.BF.1: Write a function that describes a relationship between two quantities.
 \*\*F.BF.1a: Determine an explicit expression, a recursive process, or steps for calculation from a context.
 \*\*F.BF.1b: Combine standard function types using arithmetic operations. This involves transformation of a function.

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 July 2015

**F.BF.2:** Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations from a variety of contexts (e.g., science, history, and culture), including those from the Montana American Indian, and translate between the two forms.

#### **\*\*F.BF.4:** Find inverse functions.

**\*\*F.BF.4a:** Solve an equation of the form *f*(*x*) = *c* for a simple function *f* that has an inverse and write an expression for the inverse.

#### **Unit 2A Module 8: Modeling with Linear Functions**

#### S.ID.6, S.ID.7, S.ID.8, S.ID.9

S.ID.6: Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.
 \*\*S.ID.6a: Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.

**\*\*S.ID.6b:** Informally assess the fit of a function by plotting and analyzing residuals.

**S.ID.6c:** Fit a linear function for a scatter plot that suggests a linear association.

S.ID.7: Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data.

**\*\*S.ID.8:** Compute (using technology) and interpret the correlation coefficient of a linear fit.

**\*\*S.ID.9:** Distinguish between correlation and causation.

#### Unit 2A Module 9: Systems of Equations and Inequalities

#### A.CED.2, A.CED.3, A.REI.5, A.REI.6, A.REI.12

**A.CED.2:** Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

**A.CED.3:** Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context.

**A.REI.5:** Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions.

**A.REI.6:** Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.

**A.REI.12:** Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersections of the corresponding half-planes.

#### **Unit 2B Module 10: Exponential Functions and Equations**

#### A.CED.1, A.SSE.3, F.BF.3, F.IF.8, F.LE.1, F.LE.2, F.LE.5

**A.CED.1:** Create equations and inequalities in one variable and use them to solve problems from a variety of contexts (e.g., science, history, & culture), including those of Montana American Indians. Include equations arising from linear and <del>quadratic</del> functions, simple rational and exponential functions.

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**A.SSE.3:** Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.

**\*\*A.SSE.3c:** Use the properties of exponents to transform expressions for exponential functions.

**F.BF.3**: Identify the effect on the graph of replacing f(x) by f(x) + k, kf(x), f(kx) and f(x+k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expression for them.

**\*\*F.IF.8:** Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.

**\*\* F.IF.8b:** Use the property of exponents to interpret expressions for exponential functions.

F.LE.1: Distinguish between situations that can be modeled with linear functions and with exponential functions.
 \*\*F.LE.1c: Recognize situations which a quantity grows or decays by a constant percent rate per unit interval relative to another.

**F.LE.2:** Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).

**F.LE.5:** Interpret the parameters in a linear or exponential function in terms of a context.

## **Unit 2B Module 11: Modeling with Exponential Functions**

## F.LE.1, F.LE.3, S.ID.6

F.LE.1: Distinguish between situations that can be modeled with linear functions and with exponential functions.

**F.LE.1a:** Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals.

**\*\*F.LE.1b:** Recognize situations in which a quantity changes at a constant rate per unit interval relative to another.

**F.LE.1c:** Recognize situations which a quantity grows or decays by a constant percent rate per unit interval relative to another.

**\*\*F.LE.3:** Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, <del>quadratically, or (more generally) as a polynomial function</del>.

S.ID.6: Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.
S.ID.6a: Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.
S.ID.6b: Informally assess the fit of a function by plotting and analyzing residuals.

# End of 1st Semester

Strikethrough means that the standard appears in a later course.

2nd Semester - Unit 3: Statistics & Data		
<ul> <li>Objectives</li> <li>The student will be able to: <ul> <li>Create and analyze frequency tables</li> <li>Joint, marginal, conditional frequency</li> </ul> </li> <li>Create and analyze histograms, box plots, &amp; dot plots</li> <li>Determine mean, median, mode, interquartile range, standard deviation, and outliers</li> <li>Create and analyze scatterplots</li> <li>Line of fit</li> <li>Interpret rate of change and intercepts</li> <li>Trends</li> <li>Correlation (+, -, no correlation) and causation</li> <li>Calculate correlation &amp; residuals</li> </ul>	<ul> <li>Essential Questions <ul> <li>How can you use the two-way table to determine the probability of a conditional event?</li> <li>How can you describe the data's shape, center and spread by looking at histograms, boxplots, and dotplots?</li> <li>What is the difference between the range and the interquartile range of a data set?</li> <li>What are the possible effects an outlier can have on shape, center, and spread of a data set?</li> <li>What guidelines make a line of good fit?</li> </ul> </li> <li>Mathematical Practices <ul> <li>1: Make sense of problems and persevere in solving them.</li> <li>2: Reason abstractly and quantitatively.</li> <li>3: Construct viable arguments and critique the reasoning of others.</li> <li>4: Model with mathematics.</li> <li>5: Use appropriate tools strategically.</li> <li>7: Look for and make use of structure.</li> <li>8: Look for and express regularity in repeated reasoning.</li> </ul> </li> </ul>	

## **Module 12: Descriptive Statistics**

#### **S.ID.5**

**\*\*S.ID.5:** Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data.

## Module 13: Data Displays

## S.ID.1, S.ID.2, S.ID.3

S.ID.1: Represent data with plots on the real number line (dot plots, histograms, and boxplots).

**\*\*S.ID.2:** Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard deviation) of two or more different data sets.

**\*\*S.ID.3:** Interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of extreme data points (outliers).

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2nd Semester - Unit 4: Polynomial Expressions & Equations		
Objectives         The student will be able to:         Define and interpret polynomials         O Factors         O Coefficients         O Degree         O Terms         Factor Quadratics         O Find zeroes         O GCF         O Difference of squares         O Regrouping         O Guess & Test is also an option         Work with operations with polynomials (include Closure)	<ul> <li>Essential Questions <ul> <li>How does factoring a quadratic predict its x-intercepts?</li> <li>How do the parameters of a quadratic equation (a, b, c, degree) affect the graph?</li> <li>Which features are highlighted in each of the forms of a quadratic equation?</li> <li>How does the discriminant predict the number of solutions?</li> <li>How does the concept of combining like terms work as it relates to operations with polynomials?</li> <li>What is the relationship of the Distributive Property and the concept of factoring out a common factor from an expression?</li> </ul> </li> </ul>	
<ul> <li>Create/Solve/Graph quadratic equations in Standard, Vertex, and Intercept Forms</li> <li>Analyze quadratic functions</li> <li>Solve quadratic equations         <ul> <li>Square roots</li> <li>Factoring</li> <li>Quadratic Formula using the discriminant</li> <li>Completing the square</li> </ul> </li> <li>Solve quadratic systems         <ul> <li>Graphically and algebraically</li> <li>Analyze the effect of parameters on quadratics</li> </ul> </li> </ul>	<ul> <li>Mathematical Practices</li> <li>1: Make sense of problems and persevere in solving them.</li> <li>2: Reason abstractly and quantitatively.</li> <li>3: Construct viable arguments and critique the reasoning of others.</li> <li>4: Model with mathematics.</li> <li>5: Use appropriate tools strategically.</li> <li>6: Attend to precision.</li> <li>7: Look for and make use of structure.</li> <li>8: Look for and express regularity in repeated reasoning.</li> </ul>	

# Module 14: Polynomials & Operations

# A.SSE.2, A.APR.1

A.SSE.2: Use the structure of an expression to identify ways to rewrite it.

**\*\*A.APR.1:** Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.

# Module 15: Factoring Polynomials

# A.SSE.2, A.SSE.3

**A.SSE.2:** Use the structure of an expression to identify ways to rewrite it.

**A.SSE.3:** Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.

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# Module 16: Solving Quadratic Equations

A.SSE.3, A.REI.4, A.REI.7, F.IF.8

**A.SSE.3:** Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.

**\*\*A.SSE.3a:** Factor a quadratic expression to reveal the zeroes of the function it defines.

**\*\*A.SSE.3b:** Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines.

**\*\*A.REI.4:** Solve quadratic equations in one variable.

**\*\*A.REI.4a:** Use the method of completing the square to transform any quadratic equation in x into an equation of the form  $(x - p)^2 = q$  that has the same solutions. Derive the quadratic formula from this form.

**\*\*A.REI.4b:** Solve quadratic equations by inspection (e.g., for  $x^2 = 49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriated to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as  $a \mp bi$  for real numbers a and b.

**\*\*A.REI.7:** Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically.

**F.IF.8:** Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.

**\*\*F.IF.8a:** Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context.

2nd Semester - Unit 5: Functions & Modeling		
Objectives         The student will be able to:         Work with rational and irrational numbers         O Informal proofs         Compare quadratic functions to linear & exponential functions         Calculate rate of change of a function         Calculate rate of change of a function         Compare/Contrast graphs of functions         O Linear         O Quadratic         Write a function in different, equivalent forms         Compare properties of 2 functions         O Graphically         O Algebraically         O Verbally         O Numerical (table)         Write functions to model a relationship between two quantities         Compare linear, exponential, and quadratic functions	<ul> <li>Essential Questions</li> <li>Given a representation (PETS), how can you determine which family the function belongs to?</li> <li>Mathematical Practices</li> </ul>	
	<ol> <li>1: Make sense of problems and persevere in solving them.</li> <li>2: Reason abstractly and quantitatively.</li> <li>3: Construct viable arguments and critique the reasoning of others.</li> <li>4: Model with mathematics.</li> <li>5: Use appropriate tools strategically.</li> <li>6: Attend to precision.</li> <li>7: Look for and make use of structure.</li> <li>8: Look for and express regularity in repeated reasoning.</li> </ol>	

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#### **Module 17: Quadratic Functions**

#### A.CED.2, A.REI.11, F.IF.4, F.IF.7, F.BF.3, F.LE.3

**A.CED.2:** Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

**A.REI.11:** Explain why the x-coordinates of the points where the graphs of the equations y = f(x) and y = g(x) intersect are the solution of the equations f(x) = g(x); find the solutions approximately, e.g., using technology to graph functions, make tables of values, or find successive approximations. Include cases where f(x) and/or g(x) are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.

**F.IF.4:** For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.

**F.IF.7:** Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology in more complicated cases.

**F.IF.7a:** Graph linear and quadratic functions and show intercepts, maxima, and minima.

\*\*FIF.7e: Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.

**F.BF.3**: Identify the effect on the graph of replacing f(x) by f(x) + k, kf(x), f(kx) and f(x+k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expression for them.

**F.LE.3:** Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, <del>quadratically, or (more generally) as a polynomial function</del>.

# Module 18: Piecewise and Absolute Value Functions

## A.CED.2, F.IF.7, F.BF.3

**A.CED.2:** Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

**F.IF.7:** Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology in more complicated cases.

**\*\*F.IF.7b:** Graph piecewise-defined functions, including step functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.

**F.BF.3**: Identify the effect on the graph of replacing f(x) by f(x) + k, kf(x), f(kx) and f(x+k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expression for them.

## **Module 19: Square Root & Cube Root Functions**

Strikethrough means that the standard appears in a later course.

## A.CED.2, F.IF.7, F.IF.9, F.BF.3

**A.CED.2:** Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.

**F.IF.7:** Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology in more complicated cases.

**F.IF.7b:** Graph piecewise-defined functions, including step functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.

**F.IF.9:** Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).

**F.BF.3:** Identify the effect on the graph of replacing f(x) by f(x) + k, kf(x), f(kx) and f(x+k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expression for them.

# End of 2nd Semester

Strikethrough means that the standard appears in a later course.